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# Single Emitter Detection with Fluorescence and Extinction Spectroscopy

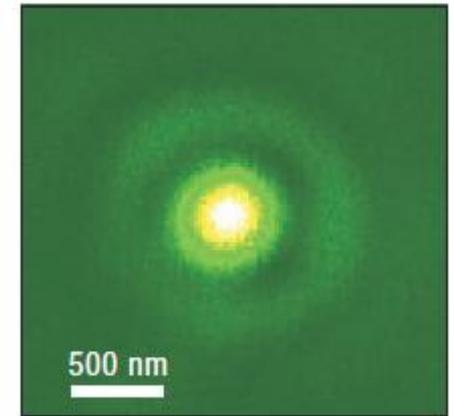
Michael Krall

Elements of Nanophotonics  
Associated Seminar „Recent Progress in Nanooptics & Photonics“

May 07, 2009

# Outline

- ❖ Single molecule fluorescence detection
- ❖ Single molecule extinction measurements
- ❖ Theoretical limits
- ❖ Comparison in terms of SNR
- ❖ Single quantum dot spectroscopy
- ❖ Outlook

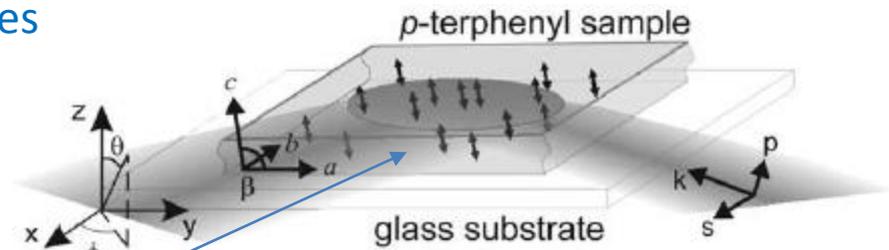


*Laser scan image of a single molecule  
(FWHM focus spot  $\approx 370$  nm).*

# Single molecule fluorescence detection

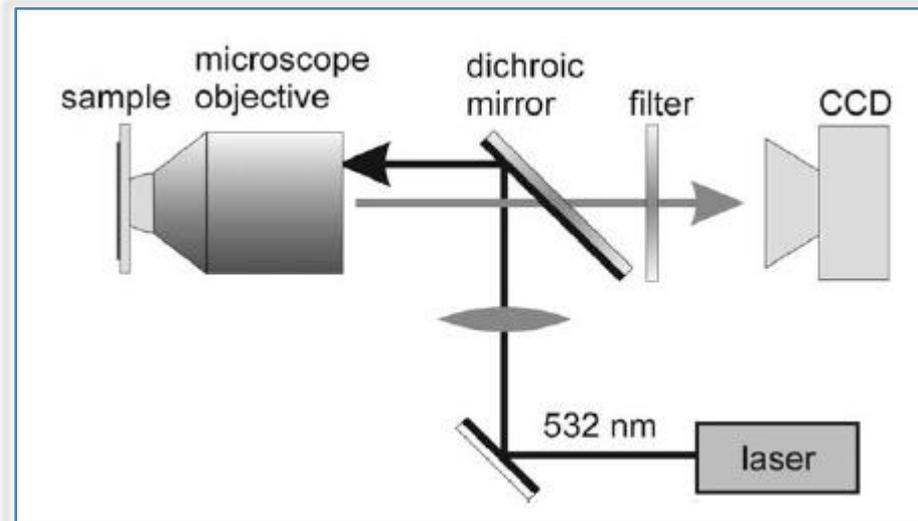
R.J. Pfab et al., Chem. Phys. Lett. 387, 490 (2004)

## ❖ Single molecule fluorescence studies



*transition dipole moments of terrylene molecules are oriented approximately perpendicular to substrate*

*p-terphenyl film on a glass substrate with dopant terrylene molecules.*

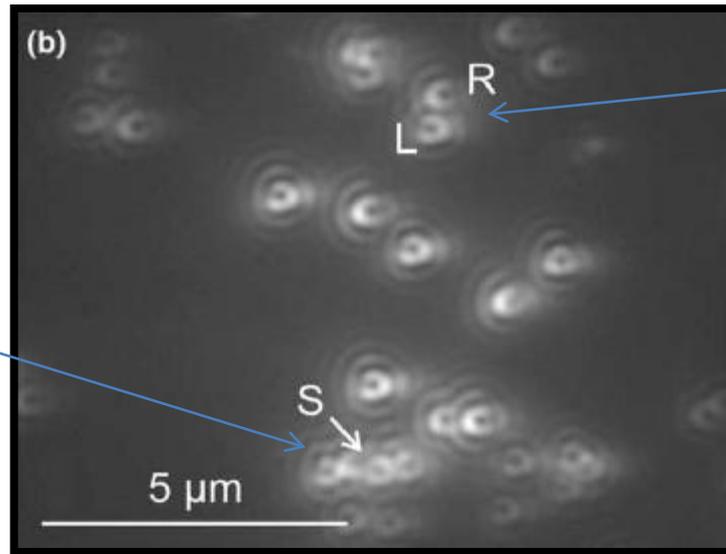


*Experimental fluorescence microscopy setup.*

# Single molecule fluorescence detection

R.J. Pfab et al., Chem. Phys. Lett. 387, 490 (2004)

## ❖ Single molecule fluorescence studies



*asymmetries attributed to a slight tilt of the emission dipole with respect to optical axis*

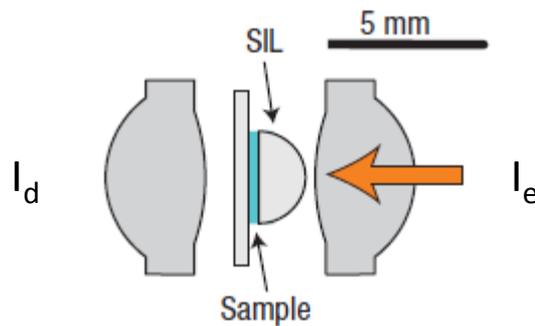
*nearly ring-like emission pattern = characteristic of vertically oriented dipoles*

*Fluorescence image.*

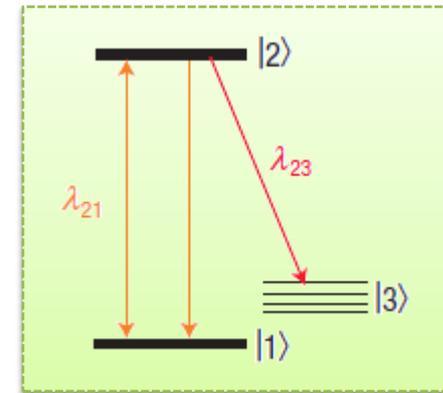
# Single molecule extinction measurements

G. Wrigge et al., *Nature Phys.* 4, 60 (2008)

## ❖ Detection of a single emitter in transmission



*Arrangement of the lenses in the illumination and collection paths.*



*Energy-level scheme of a molecule.*

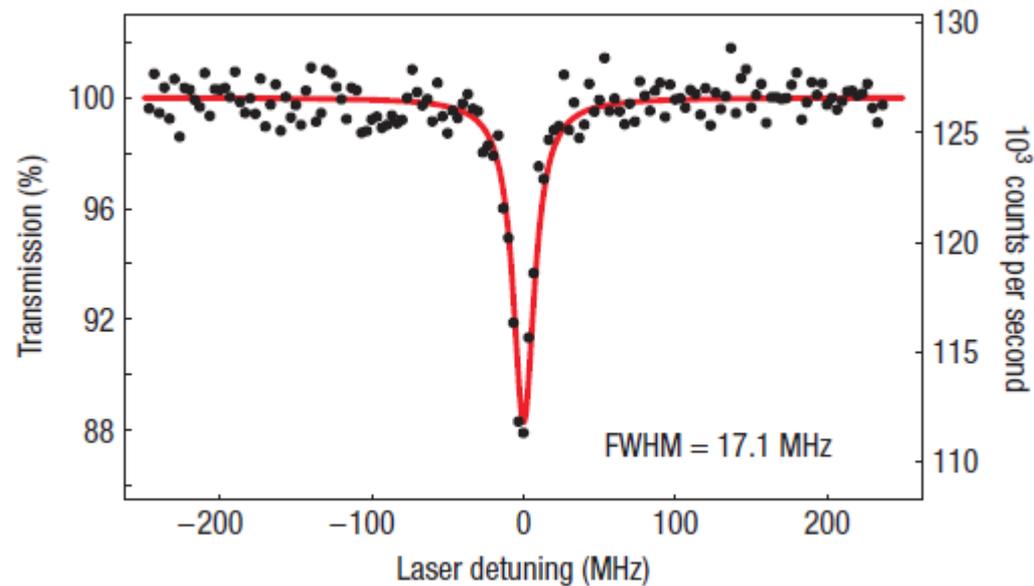
$$I_d = (1 - \sigma/F)I_e$$

$$I_d = \langle \hat{\mathbf{E}}_e^- \cdot \hat{\mathbf{E}}_e^+ \rangle + \langle \hat{\mathbf{E}}_m^- \cdot \hat{\mathbf{E}}_m^+ \rangle + 2\text{Re}\{\langle \hat{\mathbf{E}}_e^- \cdot \hat{\mathbf{E}}_m^+ \rangle\}$$

# Single molecule extinction measurements

*G. Wrigge et al., Nature Phys. 4, 60 (2008)*

## ❖ Detection of a single emitter in transmission

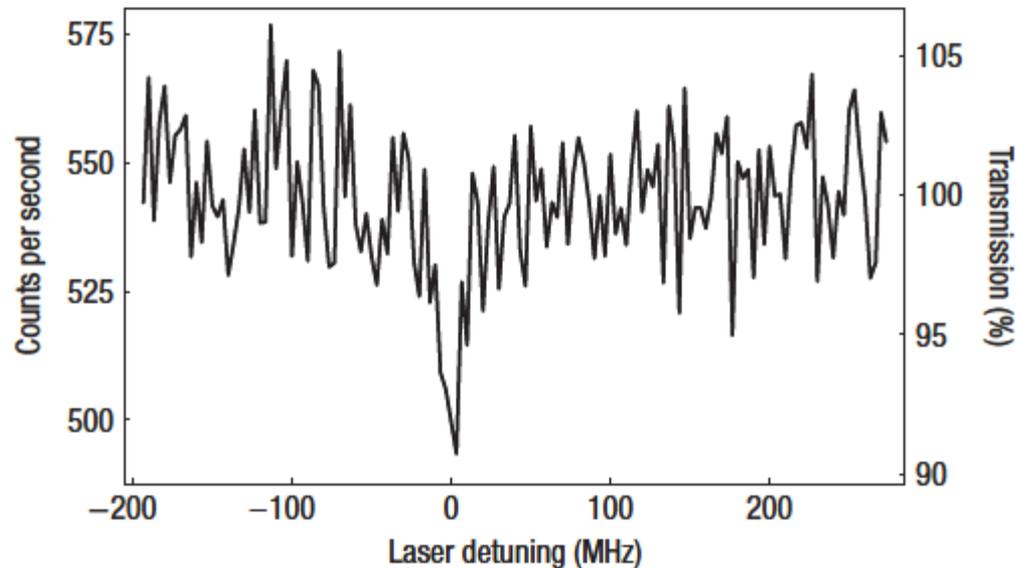


*Example of a transmission spectrum (11.5% dip).*

# Single molecule extinction measurements

*G. Wrigge et al., Nature Phys. 4, 60 (2008)*

## ❖ Single-molecule detection with ultrafaint light sources



*Extinction spectrum recorded from a single molecule under an ultrafaint detected power of **550 photons per second**.*

# Theoretical limits

G. Zumofen et al., PRL 101, 180404 (2008)

## ❖ Scattering by a classical oscillator

→ Abraham-Lorentz equation:

$$\ddot{\mathbf{q}} + \Gamma' \dot{\mathbf{q}} - \tau \ddot{\ddot{\mathbf{q}}} + \omega_0^2 \mathbf{q} = \frac{e}{m} E_0 \boldsymbol{\epsilon} e^{-i\omega_L t}$$

(see Jackson: Classical Electrodynamics)

$\mathbf{q}$  .. displacement of electron

$\Gamma'$  .. damping by non-radiative channels ( $\approx 0$ )

$E_0$  .. electric field amplitude at place of oscillator

$\boldsymbol{\epsilon}$  .. unit vector along direction of driving field  $E$

$\tau$  .. characteristic time of damping by radiation reaction

gives stationary state solution of  $\mathbf{q}$ :

$$\mathbf{q} = -\frac{e}{m\omega_0} \frac{E_0 e^{-i\omega_L t}}{2\Delta + i\Gamma} \boldsymbol{\epsilon}$$

$$\Delta = \omega_L - \omega_0$$

$$\Gamma = \tau \omega_0^2 = \frac{2e^2 \omega_0^2}{3mc^3}$$

which allows to calculate stationary state scattered far-field:

$$\mathbf{E}_{\text{sca}}(\mathbf{r}) = \frac{e}{c^2} \frac{1}{r} [\hat{\mathbf{r}} \times (\hat{\mathbf{r}} \times \ddot{\mathbf{q}})] e^{ikr}$$

$\Delta$  .. laser frequency detuning

$\Gamma$  .. damping rate

(Gaussian units)

# Theoretical limits

G. Zumofen et al., PRL 101, 180404 (2008)

## ❖ Scattering by a classical oscillator

→ total scattered power: 
$$P_{\text{sca}} = \frac{1}{2} c \epsilon_0 \int_{4\pi} r^2 |\mathbf{E}_{\text{sca}}(\mathbf{r})|^2 d\Omega = 2c W_{\text{inc}}^{\text{el}}(O) \sigma$$

where  $W_{\text{inc}}^{\text{el}}(O) = \epsilon_0 |\mathbf{E}_{\text{inc}}(O)|^2 / 4$  is the time-averaged electric energy density at O

and  $\sigma = \sigma_0 \frac{\Gamma^2}{4\Delta^2 + \Gamma^2}$  the total scattering cross section of the oscillator

$\sigma_0 = 3\lambda^2 / (2\pi)$  .. cross section at resonance: **depends only on wavelength!**

# Theoretical limits

G. Zumofen et al., PRL 101, 180404 (2008)

## ❖ Scattering by a two-level system (semi-classical description)

→ stationary state population of the upper state:

$$\rho_{22}^{\text{ss}} = \frac{\Gamma_2 \mathcal{V}^2}{2\Gamma_1 (\Delta^2 + \Gamma_2^2 + \mathcal{V}^2 \Gamma_2 / \Gamma_1)}$$

(see *Cohen-Tannoudji* et al.: Atom-Photon interactions)

$\Gamma_1$  .. radiative decay rate

$\Gamma_2$  .. damping rate of polarization

$\Gamma_2^*$  .. dephasing rate for nonradiating processes

$\mathcal{V}$  .. Rabi frequency

$d_{12}$  .. transition dipole moment

$$\Gamma_2 = \Gamma_1/2 + \Gamma_2^*$$

$$\mathcal{V} = -\mathbf{d}_{12} \cdot \mathbf{E}_{\text{inc}}(\mathbf{O})/\hbar$$

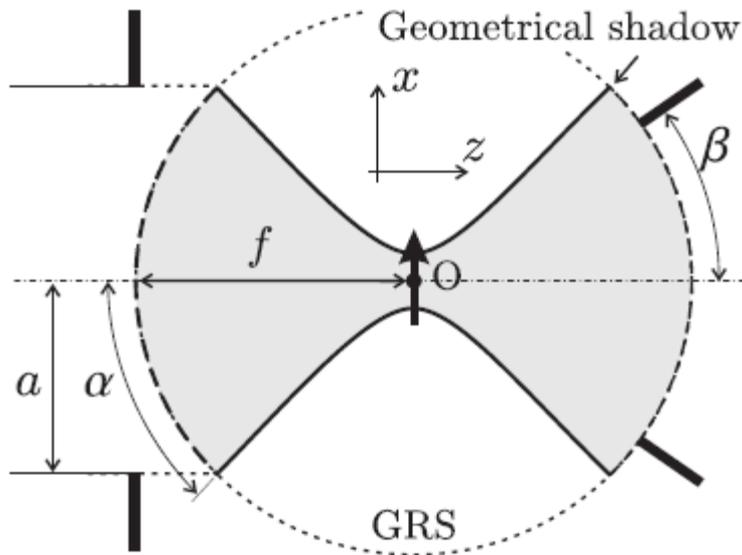
gives power scattered into solid angle of  $4\pi$ :

$$P_{\text{sca}} = \hbar\omega\Gamma_1\rho_{22}^{\text{ss}} = \sigma_0 \frac{\Gamma_1\Gamma_2}{2(\Delta^2 + \Gamma_2^2 + \mathcal{V}^2\Gamma_2/\Gamma_1)} (2cW^{\text{el}})$$

# Theoretical limits

G. Zumofen et al., PRL 101, 180404 (2008)

## ❖ Light scattering by an oscillating dipole in a focused beam



- a .. entrance-aperture radius
- $\alpha$  .. entrance half angle
- $\beta$  .. collection half angle
- f .. focal length

ratio of scattered to incident power:

$$\mathcal{K} = \frac{P_{\text{sca}}}{P_{\text{inc}}} = \frac{2cW_{\text{inc}}^{\text{el}}(O)\sigma}{\int \mathbf{S}(\mathbf{r}) \cdot \mathbf{n} d^2r} = \frac{\sigma}{\mathcal{A}}$$

effective cross section:

$$\sigma = \begin{cases} \sigma_0 \frac{\Gamma^2}{4\Delta^2 + \Gamma^2} & \text{classical oscillator} \\ \sigma_0 \frac{\Gamma_1^2}{4\Delta^2 + \Gamma_1^2 + 2\Omega^2} & \text{two-level system} \end{cases}$$

effective focal area in the case of a focused plane wave:

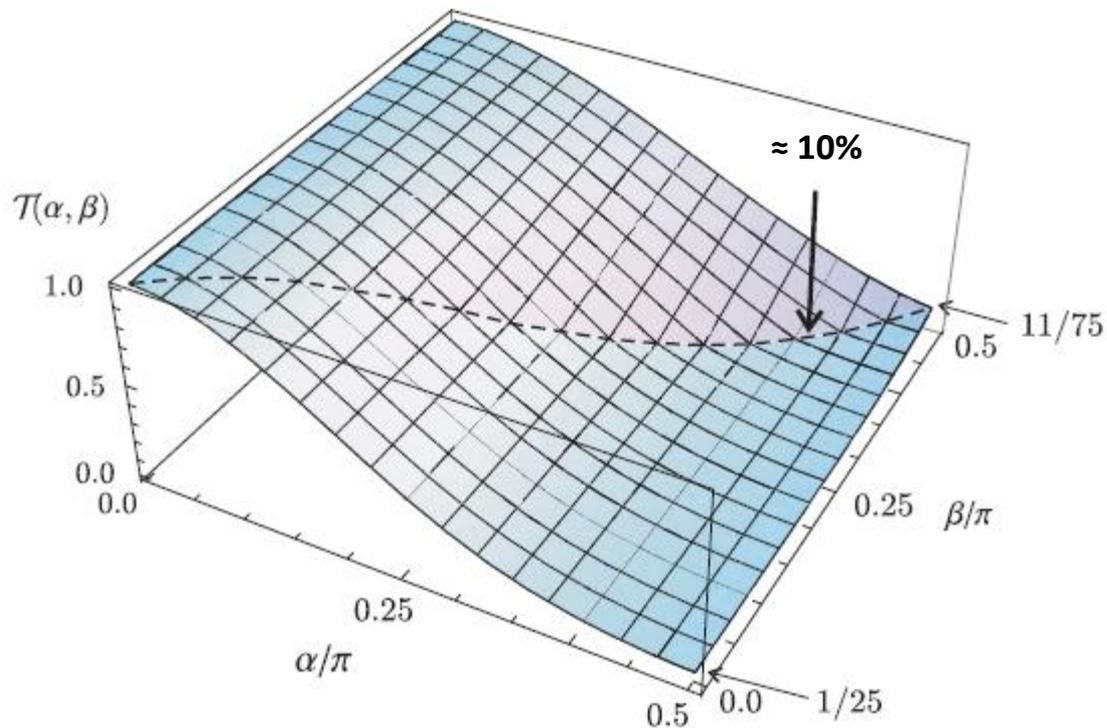
$$\mathcal{A} = \frac{\int_{\text{FP}} S_z d^2r}{S_z(O)} \quad \begin{array}{l} \text{power transmitted through focal plane} \\ \text{electric energy density at focal spot} \end{array}$$

**scattered power depends only on field strength at position of oscillator!**

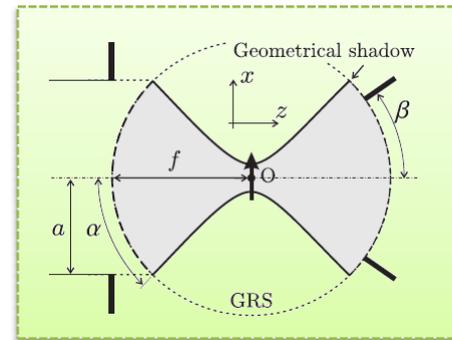
# Theoretical limits

G. Zumofen et al., PRL 101, 180404 (2008)

## ❖ Light scattering by an oscillating dipole in a focused beam



Transmittance of a focused plane wave as a function of the angles  $\alpha$  and  $\beta$ .



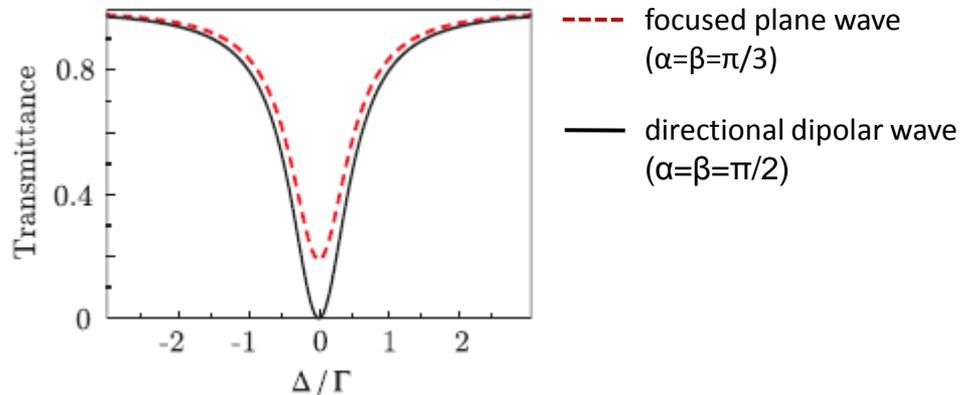
- $a$  .. entrance-aperture radius
- $\alpha$  .. entrance half angle
- $\beta$  .. collection half angle
- $f$  .. focal length

➔ focused plane wave can be attenuated up to 90%!

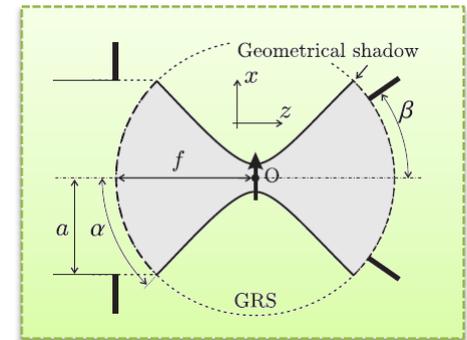
# Theoretical limits

G. Zumofen et al., PRL 101, 180404 (2008)

## ❖ Light scattering by an oscillating dipole in a focused beam



Transmittance as a function of the detuning.



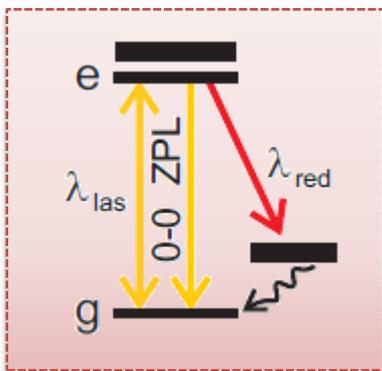
$a$  .. entrance-aperture radius  
 $\alpha$  .. entrance half angle  
 $\beta$  .. collection half angle  
 $f$  .. focal length

➔ **directional dipolar wave can be completely attenuated!**

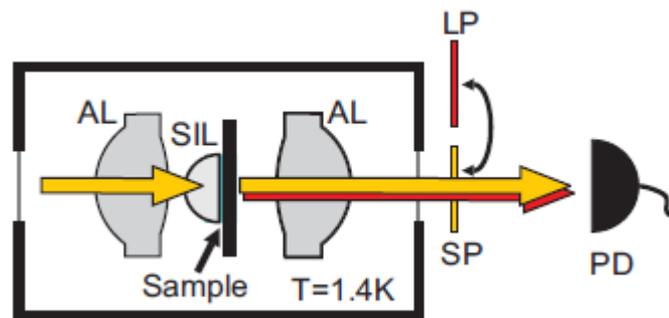
# Comparison in terms of SNR

G. Wrigge et al., *Opt. Express* 16, 17360 (2008)

## ❖ Limits of single emitter detection in fluorescence and extinction



Level scheme of a dye molecule.  
( $\lambda_{las} \approx 590 \text{ nm}$ ,  $\lambda_{red} > 600 \text{ nm}$ )



AL .. aspheric lens  
SIL .. solid immersion lens  
LP /SP.. long/short pass  
PD .. photodetector

Schematics of the experimental setup.  
(Sample: DBATT molecules embedded in a n-tetradecane matrix)

Power on PD:  
(without filter)

$$P = \frac{\epsilon_0 c r^2}{2\hbar\omega} \int_{\Omega} \left( \langle \hat{\mathbf{E}}_{las}^- \cdot \hat{\mathbf{E}}_{las}^+ \rangle + \langle \hat{\mathbf{E}}_m^- \cdot \hat{\mathbf{E}}_m^+ \rangle + 2\text{Re} \langle \hat{\mathbf{E}}_{las}^- \cdot \hat{\mathbf{E}}_m^+ \rangle \right) d\Omega$$

$$= P_{las} + P_m^{\Omega} - P_{ext},$$

laser

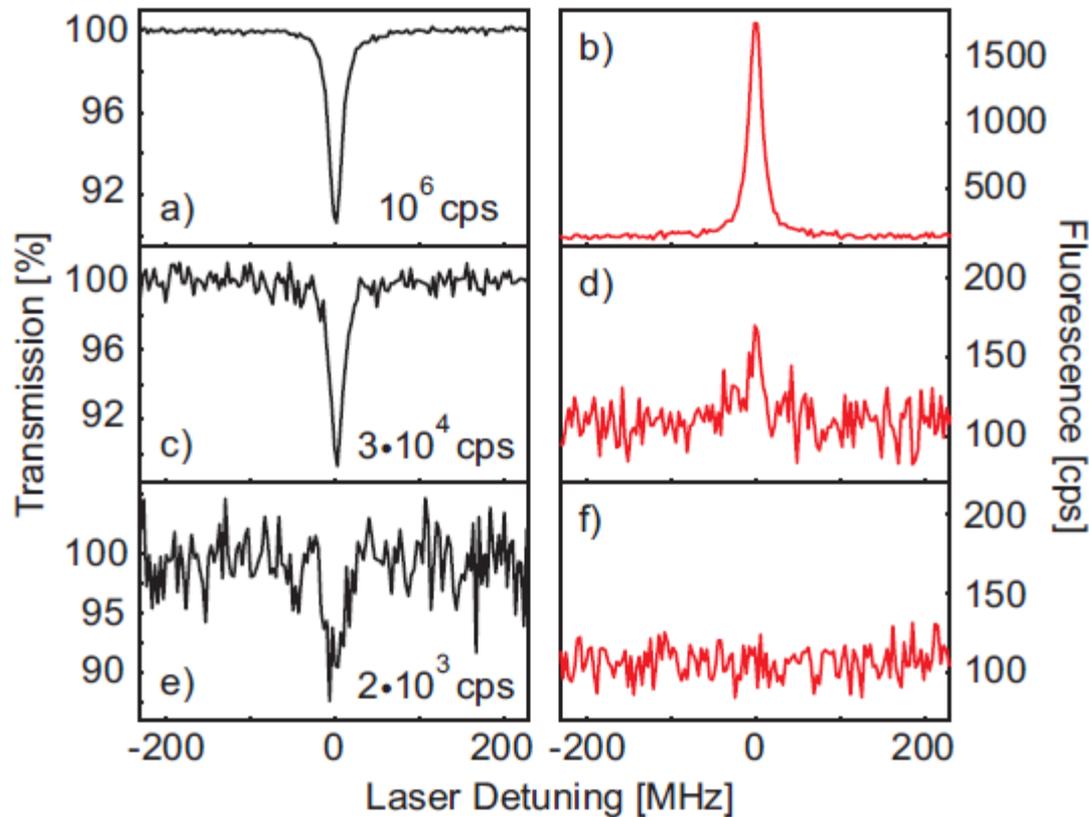
molecular  
emission

interference

# Comparison in terms of SNR

G. Wrigge et al., *Opt. Express* 16, 17360 (2008)

## ❖ Limits of single emitter detection in fluorescence and extinction



*Extinction and fluorescence excitation spectra recorded from a single molecule in transmission at three different detected laser powers.*

# Comparison in terms of SNR

G. Wrigge et al., *Opt. Express* 16, 17360 (2008)

## ❖ Limits of single emitter detection in fluorescence and extinction

Power on PD:  
(without filter)

$$P = \frac{\epsilon_0 c \tau^2}{2\hbar\omega} \int_{\Omega} \left( \langle \hat{\mathbf{E}}_{\text{las}}^- \cdot \hat{\mathbf{E}}_{\text{las}}^+ \rangle + \langle \hat{\mathbf{E}}_{\text{m}}^- \cdot \hat{\mathbf{E}}_{\text{m}}^+ \rangle + 2\text{Re} \langle \hat{\mathbf{E}}_{\text{las}}^- \cdot \hat{\mathbf{E}}_{\text{m}}^+ \rangle \right) d\Omega$$

$$= P_{\text{las}} + P_{\text{m}}^{\Omega} - P_{\text{ext}},$$

$$P_{\text{m}}^{A\pi} = \Gamma_1 \rho_{22} = \frac{\Gamma_1}{2} \frac{S}{1+S} \quad P_{\text{m}}^{\Omega} = \zeta P_{\text{m}}^{A\pi}$$

resonant:  $P_{\text{m}}^{\text{res}} = \alpha P_{\text{m}}^{\Omega}$

red-shifted:  $P_{\text{m}}^{\text{red}} = (1 - \alpha) P_{\text{m}}^{\Omega}$

$\alpha$  .. power emitted on 0-0 ZPL to total excited state emission  
 $\Gamma_1$  .. total spontaneous emission rate  
 $\Gamma_2$  .. transverse decay rate

Saturation parameter:  $S = \frac{\alpha}{\Gamma_2} \mathcal{K} P_{\text{las}}$

$\zeta$  .. collected fraction of total emitted molecular power  
 $\mu$  .. account for losses and detector efficiency  
 $\mathcal{K}$  .. ratio of scattered to incident power

# Comparison in terms of SNR

G. Wrigge et al., *Opt. Express* 16, 17360 (2008)

## ❖ SNR for a fluorescence excitation measurement

$$\text{SNR}_{\text{red}} = \frac{\mu P_{\text{m}}^{\text{red}}}{N_{\text{red}}} = \begin{cases} \frac{\mu \zeta (1 - \alpha) \Gamma_1}{2 \sqrt{P_{\text{drk}}}} \frac{S}{1 + S}, & \mu P_{\text{red}} \ll P_{\text{drk}} \\ \sqrt{\frac{\mu \zeta (1 - \alpha) \Gamma_1}{2}} \frac{S}{1 + S}, & \mu P_{\text{red}} \gg P_{\text{drk}} \end{cases}$$

*noise sources:*

- shot noise of the fluorescence
- fluctuations in the detectors dark counts

## ❖ SNR for an extinction measurement

$$\text{SNR}_{\text{res}} = \frac{\mu P_{\text{dip}}^{\text{res}}}{N_{\text{res}}} \simeq (1 - \zeta \alpha) \frac{\Gamma_1}{2} \sqrt{\frac{\mu \alpha \mathcal{K}}{\Gamma_2}} \frac{\sqrt{S}}{1 + S} \quad P_{\text{dip}}^{\text{res}} = P_{\text{ext}} - P_{\text{m}}^{\text{res}}$$

*noise sources:*

- shot noise of the detected signal
- fluctuations on the laser intensity
- fluctuations on the detector dark counts

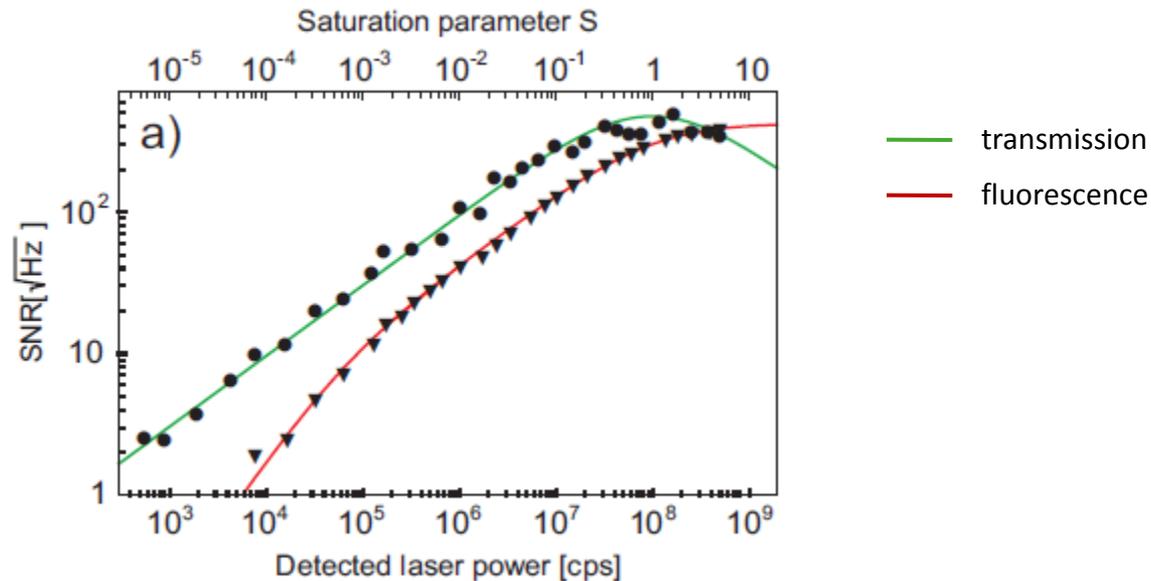
total noise  $\approx$  shot noise of laser

# Comparison in terms of SNR

G. Wrigge et al., *Opt. Express* 16, 17360 (2008)

## ❖ SNR for fluorescence excitation vs. extinction measurements

$\mu = 0.2$   
 $K = 0.5$  (strong focusing!)  
 $\alpha = 0.2$   
 $\zeta = 0.02$   
 $\Gamma_2 = \Gamma_1/2$   
 $\Gamma_1/2\pi = 17$  MHz



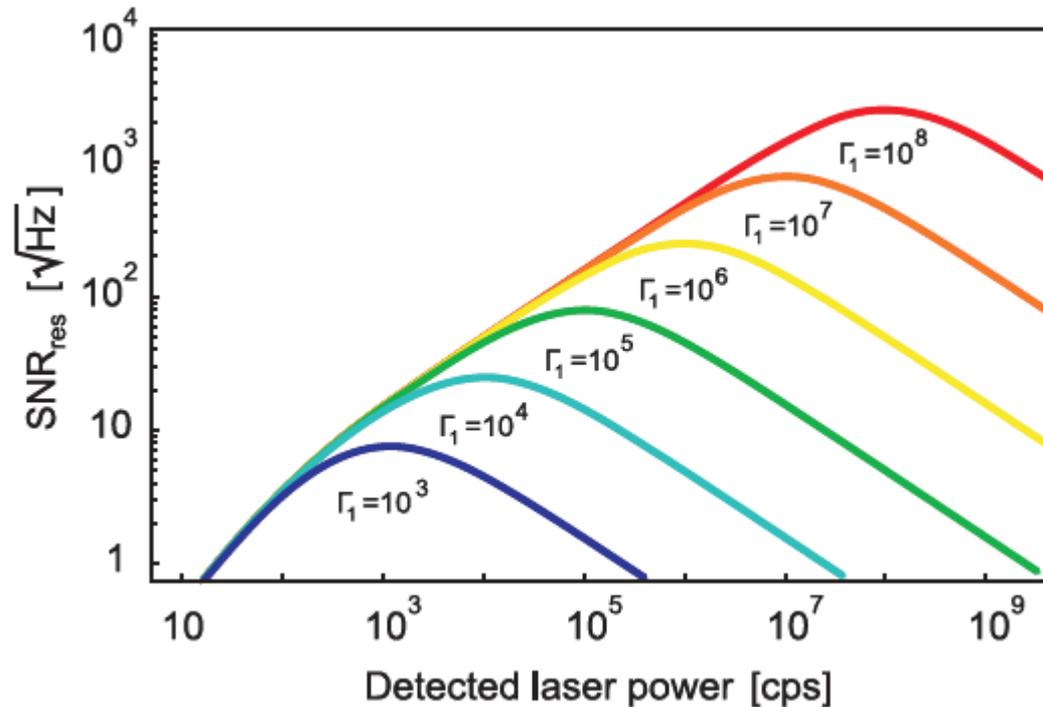
*Signal-to-noise ratios of the resonant transmission and fluorescence signals as a function of the excitation power and saturation parameter.*

➔ SNR of extinction measurements wins in the case of stronger excitations up to saturation!

# Comparison in terms of SNR

G. Wrigge et al., *Opt. Express* 16, 17360 (2008)

## ❖ Limit of extinction measurements



$\mu = 1$   
 $K = 0.5$  (strong focusing!)  
 $\alpha = 1$   
 $\Gamma_2 = \Gamma_1/2$

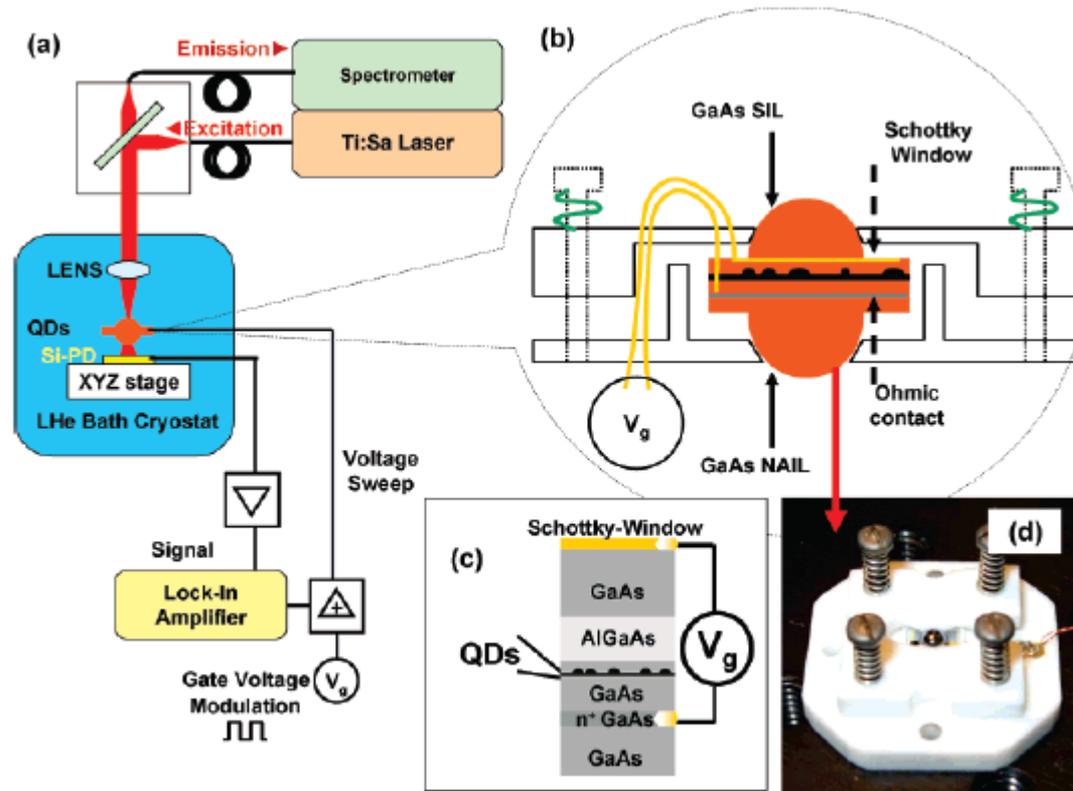
*The SNR for a resonant transmission detection of emitters with different radiative decay rates.*

➔ single emitters with spontaneous emission times as long as a millisecond detectable using extinction spectroscopy!

# Single quantum dot spectroscopy

A.N. Vamivakas et al., *Nano Lett.* 7, 2892 (2007)

- ❖ Strong extinction of a far-field laser beam by a single quantum dot

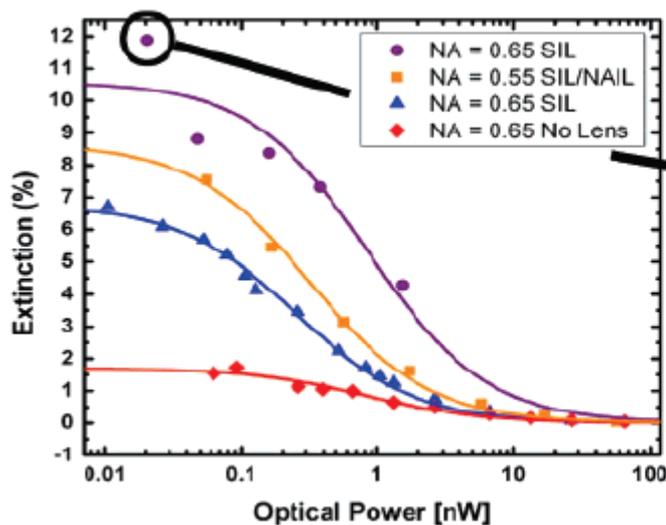


*Illustration of the experimental apparatus used for both microphotoluminescence and resonant scattering measurements.*

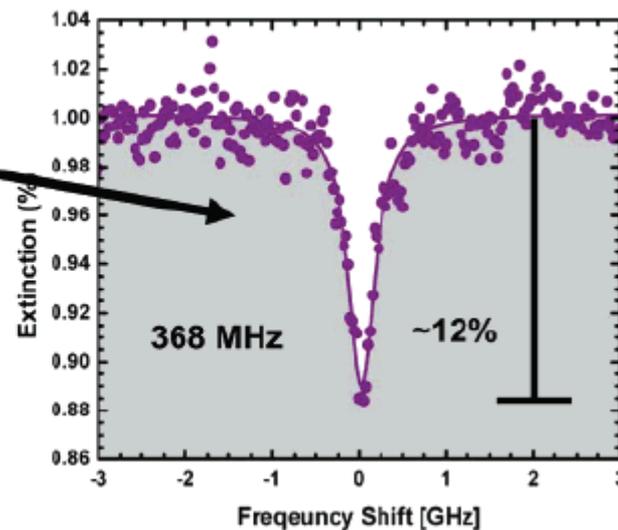
# Single quantum dot spectroscopy

A.N. Vamivakas et al., Nano Lett. 7, 2892 (2007)

- ❖ Strong extinction of a far-field laser beam by a single quantum dot



*Strength of the scattered light signal as a function of incident laser power.*



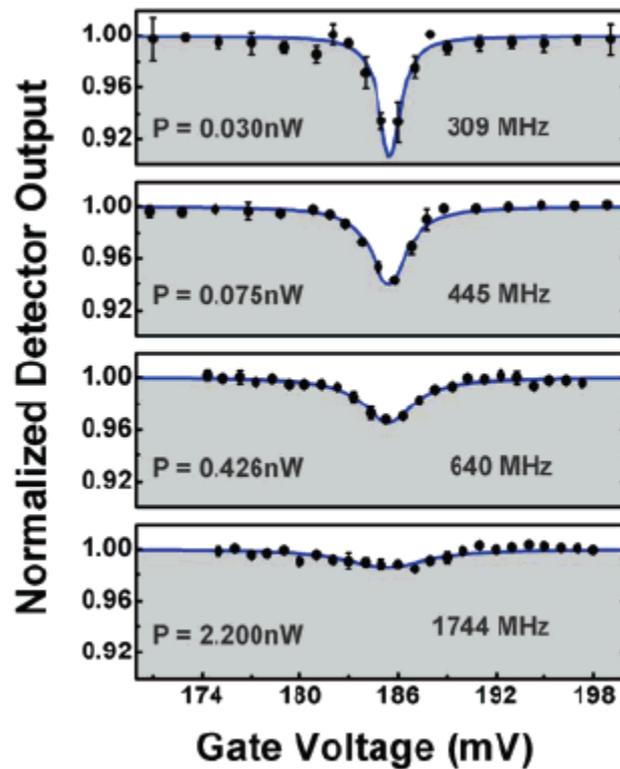
*Best line scan recorded for the lowest power point.*

➡ The measured contrast is 12% and the line width is 368 MHz (1.47  $\mu\text{eV}$ ).

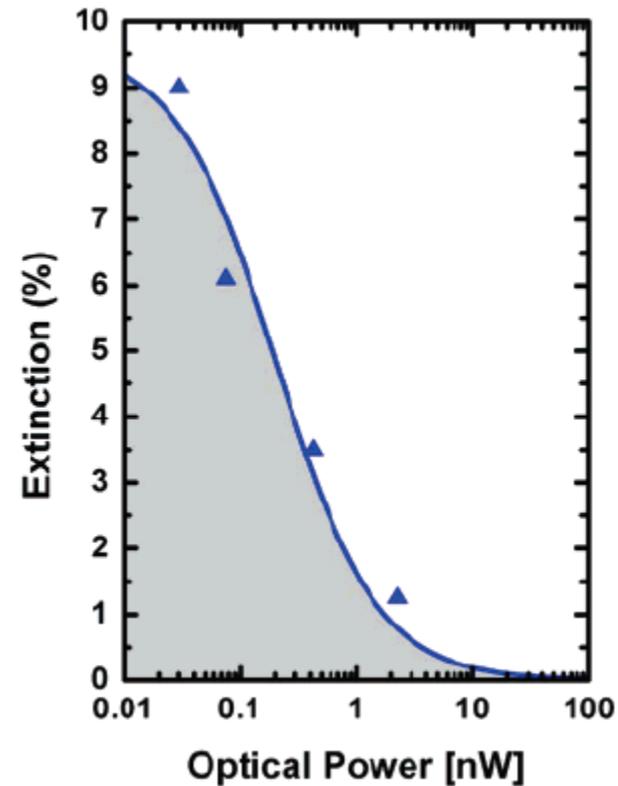
# Single quantum dot spectroscopy

A.N. Vamivakas et al., *Nano Lett.* 7, 2892 (2007)

- ❖ Strong extinction of a far-field laser beam by a single quantum dot



*Line scans as a function of incident laser power to demonstrate power broadening of the QD  $X^0$  transition.*



*Saturation curve.*

# Conclusions & Outlook

- ❖ single emitters with **spontaneous emission times** as long as **milliseconds** detectable
- ❖ direct access to **coherent interaction** of incident light and emitter
- ❖ detection of single solid-state quantum emitters at **room temperature**
- ❖ imaging of small metallic and dielectric nanoparticles
- ❖ possibility for a **strong coupling** of few photons with a single quantum emitter

# Thanks for your attention!

## References:

- R.J. Pfab et al., Chem. Phys. Lett. 387, 490 (2004)*
- G. Wrigge et al., Nature Phys. 4, 60 (2008)*
- G. Zumofen et al., PRL 101, 180404 (2008)*
- G. Wrigge et al., Opt. Express 16, 17360 (2008)*
- A.N. Vamivakas et al., Nano Lett. 7, 2892 (2007)*